## Ohio's State Tests

IHEM RELEASE

SPRING 2016
GRADE 1
MATHEMATICS

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## Grade 7 Math <br> Spring 2016 Item Release <br> Content Summary and Answer Key

| Question No. | Item Type | Content Cluster | Content Standard | Answer Key | Points |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Equation Item | Apply and <br> extend <br> previous <br> understandings <br> of operations <br> with fractions. | Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram. <br> b. Understand $p+q$ as the number located a distance $\|q\|$ from $p$, in the positive or negative direction depending on whether $q$ is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing realworld contexts. (7.NS.1b) | --- | 1 point |
| 2 | Multiple Choice | Apply and extend previous understandings of operations with fractions. | Apply and extend previous understandings of operations with fractions to add, subtract, multiply and divide rationale numbers. <br> d. Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in Os or eventually repeats. <br> (7.NS.2d) | B | 1 point |
| 3 | Multiple Choice | Draw informal comparative inferences about two populations. | Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. For example, decide whether the words in a chapter of a seventh-grade science book are generally longer than the words in a chapter of a fourth-grade science book. (7.SP.4) | D | 1 point |

## Grade 7 Math <br> Spring 2016 Item Release <br> Content Summary and Answer Key

| Question No. | Item Type | Content Cluster | Content Standard | Answe Key | Points |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | Equation Item | Analyze proportional relationships and use them to solve realworld and mathematical problems. | Recognize and represent proportional relationships between quantities. <br> c. Represent proportional relationships by equations. For example, if total cost $t$ is proportional to the number $n$ of items purchased at a constant price p , the relationship between the total cost and the number of items can be expressed as $t=p n \cdot(7 . R P .2 \mathrm{C})$ |  <br>  <br>  <br> ---1 | 1 point |
| 5 | Matching Item | Draw construct, and describe geometrical figures and describe the relationships between them. | Describe the twodimensional figures (cross sections) that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids. (7.G.3) | --- | 1 point |
| 6 | Equation Item | Analyze proportional relationships and use them to solve realworld and mathematical problems. | Recognize and represent proportional relationships between quantities. <br> b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. (7.RP.2b) | --- | 1 point |

## Grade 7 Math

Spring 2016 Item Release
Content Summary and Answer Key

| Question No. | Item <br> Type | Content Cluster | Content Standard | Answer Key | Points |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | Equation Item | Solve real-life and mathematical problems involving angle measure, area, surface area, and volume. | Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle. (7.G.4) | --- | 1 point |
| 8 | Multiple Choice | Solve real-life and mathematical problems using numerical and algebraic expressions and equations. | Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities. <br> a. Solve word problems leading to equations of the form $p x+q=r$ and $p(x+q)=r$, where $p, q$, and $r$ are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm . Its length is 6 cm . What is its width? (7.EE.4a) | C | 1 point |
| 9 | Equation Item | Analyze proportional relationships and use them to solve realworld and mathematical problems. | Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. For example, if a person walks $1 / 2$ mile in each $1 / 4$ hour, compute the unit rate as the complex fraction ${ }^{\frac{1}{2}} / \frac{1}{4}$ miles per hour, equivalently 2 miles per hour. (7.RP.1) | --- | 1 point |

## Grade 7 Math <br> Spring 2016 Item Release <br> Content Summary and Answer Key

| Question No. | Item Type | Content Cluster | Content Standard | Answer Key | Points |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | Equation Item | Analyze proportional relationships and use them to solve realworld and mathematical problems. | Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. For example, if a person walks $1 / 2$ mile in each 1/4 hour, compute the unit rate as the complex fraction ${ }^{\frac{1}{2}} / \frac{1}{4}$ miles per hour, equivalently 2 miles per hour. (7.RP.1) | --- | 1 point |
| 11 | Equation Item | Draw, construct, and describe geometrical figures and describe the relationships between them. | Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale. (7.G.1) | --- | 1 point |
| 12 | Equation Item | Analyze proportional relationships and use them to solve realworld and mathematical problems. | Recognize and represent proportional relationships between quantities. <br> b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. (7.RP.2b) | --- | 1 point |

## Grade 7 Math Spring 2016 Item Release Content Summary and Answer Key

| Question No. | Item Type | Content Cluster | Content Standard | Answer Key | Points |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | Equation Item | Solve real-life and mathematical problems using numerical and algebraic expressions and equations. | Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities. <br> a. Solve word problems leading to equations of the form $\mathrm{px}+\mathrm{q}$ $=r$ and $p(x+q)=r$, where $p, q$, and $r$ are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm . Its length is 6 cm . What is its width? (7.EE.4a) | --- | 1 point |
| 14 | Equation Item | Solve real-life and mathematical problems involving angle measure, area, surface area, and volume. | Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle. (7.G.4) | --- | 1 point |

## Grade 7 Math

Spring 2016 Item Release
Content Summary and Answer Key

| Question No. | Item Type | Content Cluster | Content Standard | Answer Key | Points |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | Equation Item | Analyze proportional relationships and use them to solve realworld and mathematical problems. | Recognize and represent proportional relationships between quantities. <br> b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. (7.RP.2b) | ---1 | 1 point |
| 16 | Multiple Choice | Analyze proportional relationships and use them to solve realworld and mathematical problems. | Recognize and represent proportional relationships between quantities. <br> a. Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin. (7.RP.2a) | D | 1 point |

# Grade 7 Math <br> Spring 2016 Item Release 

Question 1

Question and Scoring Guidelines

## Question 1

Two points, $A$ and $B$, are labeled on the number line.


What is the value of $A+B$ ?


## Points Possible: 1

Content Cluster: Apply and extend previous understandings of operations with fractions.

Content Standard: Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.
b. Understand $p+q$ as the number located a distance $|q|$ from $p$, in the positive or negative direction depending on whether $q$ is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts. (7.NS.1b)

Calculator Designation: Calculator neutral
(can appear on either part of the assessment)

## Scoring Guidelines

Exemplar Response

- 0


## Other Correct Responses

- N/A

For this item, a full-credit response includes:

- The correct sum (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 1

Sample Responses

## Sample Response: 1 point

Two points, $A$ and $B$, are labeled on the number line.


What is the value of $A+B$ ?


## Notes on Scoring

This response earns full credit ( 1 point) because the student correctly added the number -2 and its opposite to get 0.

## Sample Response: 0 points

Two points, $A$ and $B$, are labeled on the number line.


What is the value of $A+B$ ?


## Notes on Scoring

This response earns no credit (0 points) because the student incorrectly added the number -2 and its opposite. The student may have incorrectly added -2 and 2 to get 1 .

## Sample Response: 0 points

Two points, $A$ and $B$, are labeled on the number line.


What is the value of $A+B$ ?


## Notes on Scoring

This response earns no credit (0 points) because the student incorrectly added the number -2 and its opposite. The student may have incorrectly divided -2 and 2 to get -1 .

# Grade 7 Math <br> Spring 2016 Item Release 

Question 2

Question and Scoring Guidelines

## Question 2

A fraction is shown.
$\frac{5}{9}$
Which number is equivalent to the fraction?
(A) 0.5
(B) $0 . \overline{5}$
(C) $0 . \overline{59}$
(D) 5.9

## Points Possible: 1

Content Cluster: Apply and extend previous understandings of operations with fractions to add, subtract, multiply and divide rationale numbers.

Content Standard: Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.
d. Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in Os or eventually repeats. (7.NS.2d)

Calculator Designation: No calculator

## Scoring Guidelines

Rationale for Option A: This is incorrect. The student may have thought that the 5 does not repeat.

Rationale for Option B: Key - The student correctly selected the decimal equivalent.

Rationale for Option C: This is incorrect. The student may have thought that both digits in the fraction repeat.

Rationale for Option D: This is incorrect. The student may have replaced the fraction bar with a decimal point.

## Sample Response: 1 point

A fraction is shown.
$\frac{5}{9}$
Which number is equivalent to the fraction?
(A) 0.5

- $0 . \overline{5}$
(C) $0 . \overline{59}$
(D) 5.9


# Grade 7 Math <br> Spring 2016 Item Release 

Question 3

Question and Scoring Guidelines

## Question 3

Which pair of data sets provides no evidence that the values of Set A are greater than the values of Set B?
(4) Set A:

(B) Set A:


Set B

(C) Set A:

(D) Set A:


Set B:


## Points Possible: 1

Content Cluster: Draw informal comparative inferences about two populations.

Content Standard: Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. For example, decide whether the words in a chapter of a seventh-grade science book are generally longer than the words in a chapter of a fourthgrade science book. (7.SP.4)

Calculator Designation: Calculator neutral (can appear on either part of the assessment)

## Scoring Guidelines

Rationale for Option A: This is incorrect. The student may have interpreted the large spread in Set B to mean there is no evidence.

Rationale for Option B: This is incorrect. The student may have selected the plots with low evidence rather than the plots with no evidence.

Rationale for Option C: This is incorrect. The student may have selected the plots with high evidence rather than the plots with no evidence.

Rationale for Option D: Key - The student identified a large amount of spread and overlap to yield no evidence.

Sample Response: 1 point

Which pair of data sets provides no evidence that the values of Set $A$ are greater than the values of Set B?
(4) Set A:

(B) Set A:


Set B:

(C) Set A:


- Set A:



## Grade 7 Math Spring 2016 Item Release <br> Question 4

Question and Scoring Guidelines

## Question 4

Mary buys $p$ peaches at the farmer's market for $d$ dollars each. She spends a total of $t$ dollars on peaches. Create an equation that represents the relationship between $t$ and $p$.


## Points Possible: 1

Content Cluster: Analyze proportional relationships and use them to solve real-world and mathematical problems.

Content Standard: Recognize and represent proportional relationships between quantities.
c. Represent proportional relationships by equations. For example, if total cost $\dagger$ is proportional to the number $n$ of items purchased at a constant price $p$, the relationship between the total cost and the number of items can be expressed as $\dagger=p n$. (7.RP.2c)

Calculator Designation: Calculator neutral
(can appear on either part of the assessment)

## Scoring Guidelines

## Exemplar Response

- $t=d p$


## Other Correct Responses

- Any equivalent equation.

For this item, a full-credit response includes:

- The correct equation (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 4

Sample Responses

## Sample Response: 1 point

Mary buys $p$ peaches at the farmer's market for $d$ dollars each. She spends a total of $t$ dollars on peaches.
Create an equation that represents the relationship between $t$ and $p$.


## Notes on Scoring

This response earns full credit (1 point) because the student represented the proportional relationship with a correct equation.

## Sample Response: 1 point

Mary buys $p$ peaches at the farmer's market for $d$ dollars each. She spends a total of $t$ dollars on peaches. Create an equation that represents the relationship between $t$ and $p$.
$\frac{t}{d}=p$


## Notes on Scoring

This response earns full credit (1 point) because the student represented the proportional relationship with a correct equation.

## Sample Response: 0 points

Mary buys $p$ peaches at the farmer's market for $d$ dollars each. She spends a total of $t$ dollars on peaches.
Create an equation that represents the relationship between $t$ and $p$.
$t=\frac{p}{d}$


## Notes on Scoring

This response earns no credit (0 points) because the student represented the proportional relationship with an incorrect equation. The student may have incorrectly thought that the number of peaches needed to be divided by the cost of each peach to get the total.

## Sample Response: 0 points

Mary buys $p$ peaches at the farmer's market for $d$ dollars each. She spends a total of $t$ dollars on peaches.
Create an equation that represents the relationship between $t$ and $p$.
$t=\frac{d}{p}$


## Notes on Scoring

This response earns no credit (0 points) because the student represented the proportional relationship with an incorrect equation. The student may have incorrectly thought that the cost of each peach needed to be divided by the number of peaches bought to get the total.

# Grade 7 Math <br> Spring 2016 Item Release 

Question 5

Question and Scoring Guidelines

## Question 5



Select the shape that is formed by each cross section.

|  | Hexagon | Rectangle |
| :--- | :---: | :---: |
| Cross section through points $\boldsymbol{C}, \boldsymbol{D}$, and $\boldsymbol{H}$ | $\square$ | $\square$ |
| Cross section through points $\boldsymbol{A}, \boldsymbol{I}$, and $\boldsymbol{J}$ | $\square$ | $\square$ |
| Cross section through points $\boldsymbol{A}, \boldsymbol{B}, \boldsymbol{E}$, and $\boldsymbol{J}$ | $\square$ | $\square$ |

## Points Possible: 1

Content Cluster: Draw construct, and describe geometrical figures and describe the relationships between them.

Content Standard: Describe the two-dimensional figures (cross sections) that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids. (7.G.3)

Calculator Designation: Calculator neutral (can appear on either part of the assessment)

## Scoring Guidelines

For this item, a full-credit response includes:

- "Rectangle" selected for "Cross section through points C, D and H";

AND

- "Hexagon" selected for "Cross section through points A, I and J"; AND
- "Rectangle" selected for "Cross section through points $A, B, E$ and J" (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 5

Sample Responses

## Sample Response: 1 point

> A hexagonal prism is shown.


Select the shape that is formed by each cross section.

|  | Hexagon | Rectangle |
| :--- | :---: | :---: |
| Cross section through points $C, D$, and $H$ | $\square$ | $\square$ |
| Cross section through points $A, I$, and $J$ | $\square$ | $\square$ |
| Cross section through points $A, B, E$, and $J$ | $\square$ | $\square$ |

## Notes on Scoring

This response earns full credit (1 point) because the student correctly identified all three shapes of the cross sections that are the result of slicing the three dimensional figure through the given points.

## Sample Response: 0 points

A hexagonal prism is shown.


Select the shape that is formed by each cross section.

|  | Hexagon | Rectangle |
| :--- | :---: | :---: |
| Cross section through points $C, D$, and $H$ | $\square$ | $\square$ |
| Cross section through points $A, I$, and $J$ | $\boxed{ }$ | $\square$ |
| Cross section through points $A, B, E$, and $J$ | $\square$ | $\square$ |

## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly identify all three shapes for the cross sections. The student may have thought that the slice through points $A, B, E$ and $J$ results in a hexagon, when it actually results in a rectangle. All three shapes need to be identified correctly to earn credit.

## Sample Response: 0 points

A hexagonal prism is shown.


Select the shape that is formed by each cross section.

|  | Hexagon | Rectangle |
| :--- | :---: | :---: |
| Cross section through points $C, D$, and $H$ | $\square$ | $\square$ |
| Cross section through points $A, I$, and $J$ | $\square$ | $\square$ |
| Cross section through points $A, B, E$, and $J$ | $\square$ | $\square$ |

## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly identify all three shapes for the cross sections. The student may have thought that the slice through points $A, I$, and $J$ results in a rectangle, when it actually results in a hexagon. All three shapes need to be identified correctly to earn credit.

# Grade 7 Math <br> Spring 2016 Item Release 

Question 6

Question and Scoring Guidelines

## Question 6

The table shows the number of songs and the length of each music playlist on an MP3 player. Each song is the same length.

| Number of <br> Songs | Length of <br> Playlist <br> (minutes) |
| :---: | :---: |
| 4 | 16 |
| 9 | 36 |
| 16 | 64 |

How long, in minutes, is each song on the playlists?


## Points Possible: 1

Content Cluster: Analyze proportional relationships and use them to solve real-world and mathematical problems.

Content Standard: Recognize and represent proportional relationships between quantities.
b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. (7.RP.2b)

Calculator Designation: Calculator

## Scoring Guidelines

## Exemplar Response

- 4


## Other Correct Responses

- N/A

For this item, a full-credit response includes:

- The correct value (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 6

Sample Responses

## Sample Response: 1 point

The table shows the number of songs and the length of each music playlist on an MP3 player. Each song is the same length.

| Number of <br> Songs | Length of <br> Playlist <br> (minutes) |
| :---: | :---: |
| 4 | 16 |
| 9 | 36 |
| 16 | 64 |

How long, in minutes, is each song on the playlists?


## Notes on Scoring

This response earns full credit (l point) because the student correctly calculated the unit rate of 4 minutes per song: e.g.,

$$
\begin{gathered}
16 / 4=4 \\
\text { or } \\
64 / 16=4
\end{gathered}
$$

## Sample Response: 0 points

The table shows the number of songs and the length of each music playlist on an MP3 player. Each song is the same length.

| Number of <br> Songs | Length of <br> Playlist <br> (minutes) |
| :---: | :---: |
| 4 | 16 |
| 9 | 36 |
| 16 | 64 |

How long, in minutes, is each song on the playlists?


## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly calculate the unit rate of 4 minutes per song. The student may have calculated $36 / 6$ instead of $36 / 9$ to get 6 minutes instead of 4 minutes for the length of each song.

## Sample Response: 0 points

The table shows the number of songs and the length of each music playlist on an MP3 player. Each song is the same length.

| Number of <br> Songs | Length of <br> Playlist <br> (minutes) |
| :---: | :---: |
| 4 | 16 |
| 9 | 36 |
| 16 | 64 |

How long, in minutes, is each song on the playlists?


## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly calculate the unit rate of 4 minutes per song. The student may have added the two last numbers in the right column $(36+64=100)$ and then divided that number incorrectly by the sum of all three numbers in the left column ( $4+9+16=29$ ) to get $100 / 29 \approx 3.448$, and then rounded that number to 3.5 .

# Grade 7 Math <br> Spring 2016 Item Release 

Question 7

Question and Scoring Guidelines

## Question 7



What is the circumference of the circle, to the nearest tenth of a centimeter?


## Points Possible: 1

Content Cluster: Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.

Content Standard: Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle. (7.G.4)

Calculator Designation: Calculator

## Scoring Guidelines

Exemplar Response

- 31.4


## Other Correct Responses

- Any value between 31.4 and 31.43 , inclusive.

For this item, a full-credit response includes:

- A correct circumference (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 7

Sample Responses

## Sample Response: 1 point



What is the circumference of the circle, to the nearest tenth of a centimeter?
31.4


## Notes on Scoring

This response earns full credit (1 point) because the student correctly calculated the circumference of the circle. The student probably used the formula for the circumference of a circle $(2 * \pi * r=C)$, using $3.14,22 / 7$ or the $\pi$-button on a calculator for Pi , and multiplied this by 10 , the diameter ( $2 r$ ).

## Sample Response: 1 point



## Notes on Scoring

This response earns full credit (1 point) because the student correctly calculated the circumference of the circle. The student probably used the formula for the circumference of a circle ( $2 * \pi * r=C$ ), using 3.14, 22/7 or the $\pi$-button on a calculator for Pi , and multiplied this by 10 , the diameter ( $2 r$ ).

The student has responded with 31.43 , rounding to the nearest hundredth instead of to the nearest tenth. The response will still be scored with full credit (1 point), as "rounding" is not assessed in this grade. Directing the students to end with the tenths digit gives them a place value to stop writing down the decimals.

## Sample Response: 0 points



## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly calculate the circumference of the circle. The student may have rounded the value of $\pi(\mathrm{Pi})$ to 3 , which is not accepted at the middle and high school levels.
Students need to use 3.14, 22/7 or the m-button on a calculator for the value of $\pi$. If the student used the formula correctly $(2 * \pi * r=C)$, but used an incorrect value of 3 for $\pi$, the circumference may have been calculated:

$$
2 * 3 * 5=30
$$

## Sample Response: 0 points



What is the circumference of the circle, to the nearest tenth of a centimeter?

## 33



| 1 | 2 | 3 |
| :--- | :--- | :--- |
| 4 | 5 | 6 |
| 7 | 8 | 9 |
| 0 | - | - |

## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly calculate the circumference of the circle. The student may have incorrectly used 3.3 for the value of $\Pi$ (Pi). If the student used the formula correctly $(2 * \pi * r=C)$, but used an incorrect value of 3.3 for $\pi$, the circumference may have been calculated:

$$
2 * 3.3 * 5=33
$$

# Grade 7 Math <br> Spring 2016 Item Release 

Question 8

Question and Scoring Guidelines

## Question 8

A bowling alley charges $x$ dollars per guest and a fixed $\$ 50$ rental fee for parties.
Which equation represents the total cost, $y$, for 9 guests?
(A) $y=9 x$
(B) $y=9 x+41$
(C) $y=9 x+50$
(D) $y=50 x+9$

Points Possible: 1
Content Cluster: Solve real-life and mathematical problems using numerical and algebraic expressions and equations.

Content Standard: Use variables to represent quantities in a realworld or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities. a. Solve word problems leading to equations of the form $p x+q=r$ and $p(x+q)=r$, where $p, q$, and $r$ are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm . Its length is 6 cm . What is its width? (7.EE.4a)

Calculator Designation: Calculator

## Scoring Guidelines

Rationale for Option A: This is incorrect. The student may not have considered the fixed rental fee.

Rationale for Option B: This is incorrect. The student may have subtracted 9 from 50 to solve for the $y$-intercept.

Rationale for Option C: Key - The student correctly identified the equation that represents total cost.

Rationale for Option D: This is incorrect. The student may have reversed the variable and the fixed costs (9 and 50, respectively).

## Sample Response: 1 point

A bowling alley charges $x$ dollars per guest and a fixed $\$ 50$ rental fee for parties. Which equation represents the total cost, $y$, for 9 guests?
(A) $y=9 x$
(B) $y=9 x+41$
$y=9 x+50$
(D) $y=50 x+9$

# Grade 7 Math <br> Spring 2016 Item Release 

Question 9

Question and Scoring Guidelines

## Question 9

Tim is clearing brush from a large piece of land. The table shows how many acres he has cleared over time.
Brush Clearing

| Acres Cleared | Days |
| :---: | :---: |
| $\frac{2}{3}$ | 2 |
| $1 \frac{2}{3}$ | 5 |
| $2 \frac{1}{3}$ | 7 |

How many days does it take Tim to clear 1 acre?


## Points Possible: 1

Content Cluster: Analyze proportional relationships and use them to solve real-world and mathematical problems.

Content Standard: Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. For example, if a person walks 1/2 mile in each $1 / 4$ hour, compute the unit rate as the complex fraction $\frac{1}{2} / \frac{1}{4}$ miles per hour, equivalently 2 miles per hour. (7.RP.1)

Calculator Designation: Calculator

## Scoring Guidelines

Exemplar Response

- 3


## Other Correct Responses

- Any equivalent value.

For this item, a full-credit response includes:

- A correct rate (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 9

Sample Responses

## Sample Response: 1 point

Tim is clearing brush from a large piece of land. The table shows how many acres he has cleared over time.
Brush Clearing

| Acres Cleared | Days |
| :---: | :---: |
| $\frac{\mathbf{2}}{3}$ | 2 |
| $1 \frac{2}{3}$ | 5 |
| $2 \frac{1}{3}$ | 7 |

How many days does it take Tim to clear 1 acre?


## Notes on Scoring

This response earns full credit (1 point) because the student correctly calculated the number of days it takes to clear 1 acre.

## Sample Response: 1 point

Tim is clearing brush from a large piece of land. The table shows how many acres he has cleared over time.
Brush Clearing

| Acres Cleared | Days |
| :---: | :---: |
| $\frac{2}{3}$ | 2 |
| $1 \frac{2}{3}$ | 5 |
| $2 \frac{1}{3}$ | 7 |

How many days does it take Tim to clear 1 acre?


## Notes on Scoring

This response earns full credit (l point) because the student correctly identified the number of days it takes to clear 1 acre. The student may have seen that it takes 2 days to clear $2 / 3$ acres (i.e., 1 day to clear $1 / 3$ acre), calculated $2 / 3+1 / 3=1$ whole acre, and then responded with an answer of 2 days +1 day.

Sample Response: 0 points

Tim is clearing brush from a large piece of land. The table shows how many acres he has cleared over time.

## Brush Clearing

| Acres Cleared | Days |
| :---: | :---: |
| $\frac{2}{3}$ | 2 |
| $1 \frac{2}{3}$ | 5 |
| $2 \frac{1}{3}$ | 7 |

How many days does it take Tim to clear 1 acre?


## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly calculate the number of days it takes to clear 1 acre. The student may have divided $2 / 3$ by 2 to get the unit rate of $1 / 3$ acre per day, instead of the unit rate of 3 days per acre.

## Sample Response: 0 points

Tim is clearing brush from a large piece of land. The table shows how many acres he has cleared over time.
Brush Clearing

| Acres Cleared | Days |
| :---: | :---: |
| $\frac{\mathbf{2}}{3}$ | 2 |
| $1 \frac{2}{3}$ | 5 |
| $2 \frac{1}{3}$ | 7 |

How many days does it take Tim to clear 1 acre?

$$
\frac{2}{3} \div 2
$$

$$
\oplus \oplus \oplus \oplus
$$

## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly calculate the number of days it takes to clear 1 acre. The student may have started a correct process by dividing $2 / 3$ acre by 2 days to get how many acres were cleared in 1 day. However, the final answer of days to clear 1 full acre was not given.

# Grade 7 Math <br> Spring 2016 Item Release 

Question 10

Question and Scoring Guidelines

## Question 10

Cary's barbecue sauce recipe calls for $2 \frac{2}{3}$ cups of water for every 8 pints of tomato sauce.
How many cups of water does Cary use when she makes barbecue sauce with 1 pint of tomato sauce?


## Points Possible: 1

Content Cluster: Analyze proportional relationships and use them to solve real-world and mathematical problems.

Content Standard: Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. For example, if a person walks 1/2 mile in each $1 / 4$ hour, compute the unit rate as the complex fraction $\frac{1}{2} /$
$\frac{2}{2} / \frac{1}{4}$ miles per hour, equivalently 2 miles per hour. (7.RP. 1)
Calculator Designation: Calculator

## Scoring Guidelines

Exemplar Response

- $\frac{1}{3}$


## Other Correct Responses

- Any equivalent value

For this item, a full-credit response includes:

- The correct unit rate (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 10

Sample Responses

## Sample Response: 1 point



## Notes on Scoring

This response earns full credit (1 point) because the student correctly calculated the unit rate. The student may have divided 2 and $2 / 3$ by 8 , using division of fraction by a whole number. The student may have also identified that there are 8 "one-thirds" in 2 and $2 / 3$, by identifying that there are 3 "one-thirds" in each whole number and 2 "one-thirds" in 2/3.

## Sample Response: 0 points

Cary's barbecue sauce recipe calls for $2 \frac{2}{3}$ cups of water for every 8 pints of tomato sauce.
How many cups of water does Cary use when she makes barbecue sauce with 1 pint of tomato sauce?

## . 333



## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly answer with a precise unit rate. The student may have converted the fractions into decimals when calculating the unit rate. The answer would be 0.333 , with the 3 repeating.

In these cases, students are expected to convert the repeating decimal to a precise answer of $1 / 3$ (fractional form). This also applies when an answer comes out as 0.6 with the 6 repeating. Students are expected to give a precise answer of 2/3 (fractional form).

## Sample Response: 0 points

Cary's barbecue sauce recipe calls for $2 \frac{2}{3}$ cups of water for every 8 pints of tomato sauce.
How many cups of water does Cary use when she makes barbecue sauce with 1 pint of tomato sauce?
$\frac{2}{3}$
$\leftarrow \rightarrow \oplus$

4


7 | 8 | 9 |
| :--- | :--- | $<\leq>\geq$

0
. -
$\square$吅 $\pi$

## Notes on Scoring

This response earns no credit (0 points) because the student did not correctly calculate the unit rate. The student may have multiplied the whole number 2 by 8 to get 16 thirds, forgotten about the $2 / 3$ in the initial amount of cups of water and then divided by 8.

$$
\begin{aligned}
& 2 / 3 * 8=16 / 3 \\
& 16 / 3 / 8=2 / 3
\end{aligned}
$$

# Grade 7 Math <br> Spring 2016 Item Release 

Question 11
Question and Scoring Guidelines

## Question 11

Angelo drew the two rectangles shown. The second is a scale drawing of the first.

16.25 in.

What scale factor did Angelo use to draw the second rectangle?


## Points Possible: 1

Content Cluster: Draw, construct, and describe geometrical figures and describe the relationships between them.

Content Standard: Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale. (7.G.1)

Calculator Designation: Calculator

## Scoring Guidelines

Exemplar Response

- 2.5

For this item, a full-credit response includes:

- The correct scale (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 11

Sample Responses

## Sample Response: 1 point

Angelo drew the two rectangles shown. The second is a scale drawing of the first.


What scale factor did Angelo use to draw the second rectangle?
2.5



7



## Notes on Scoring

This response earns full credit (1 point) because the student calculated a correct scale factor. The student may have divided 11.25 by 4.5 and then, to check, divided 16.25 by 6.5, both times getting the scale factor of 2.5 .

## Sample Response: 0 points

Angelo drew the two rectangles shown. The second is a scale drawing of the first.

11.25 in.
16.25 in .

What scale factor did Angelo use to draw the second rectangle?
2.25


## Notes on Scoring

This response earns no credit ( 0 points) because the student did not calculate a correct scale factor. The student may have incorrectly put 10.125 into the calculator, instead of 11.25 , with the 0 being a typo (the " 0 " is right beside the " 1 " on the calculator), and not realized this mistake. Then, the student may have divided correctly by 4.5 to get an incorrect response of 2.25 . The student may have also calculated the problem correctly but made a typo in the answer, inserting an extra " 2 ".

It is important for students to check carefully that what they put into both their calculator and the answer spaces on the assessment is correct.

## Sample Response: 0 points

Angelo drew the two rectangles shown. The second is a scale drawing of the first.


What scale factor did Angelo use to draw the second rectangle?

## 4



## Notes on Scoring

This response earns no credit (0 points) because the student did not calculate a correct scale factor. The student may have incorrectly divided 4.5 by 11.25 to get 0.4 , and then checked that answer by dividing 6.5 by 16.25 , to still get 0.4. The student may have then reasoned and thought the answer must be " 4 " since the second rectangle is an enlargement.

# Grade 7 Math <br> Spring 2016 Item Release 

Question 12

Question and Scoring Guidelines

## Question 12

A dance studio offers ballet and hip-hop classes. The studio has 8 ballet classes for every 12 hip-hop classes. How many hip-hop classes are there for each ballet class?

## Points Possible: 1

Content Cluster: Analyze proportional relationships and use them to solve real-world and mathematical problems.

Content Standard: Recognize and represent proportional relationships between quantities.
b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. (7.RP.2b)

## Calculator Designation: Calculator

## Scoring Guidelines

## Exemplar Response

- 1.5


## Other Correct Responses

- Any equivalent value

For this item, a full-credit response includes:

- A correct value (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 12

Sample Responses

## Sample Response: 1 point

A dance studio offers ballet and hip-hop classes. The studio has 8 ballet classes for every 12 hip-hop classes.
How many hip-hop classes are there for each ballet class?


## Notes on Scoring

This response earns full credit (1 point) because the student determined the correct proportional relationship. The student may have divided 12 by 8 to get the proportional relationship correct.

$$
12 / 8=1.5
$$

## Sample Response: 0 points

A dance studio offers ballet and hip-hop classes. The studio has 8 ballet classes for every 12 hip-hop classes.
How many hip-hop classes are there for each ballet class?


## Notes on Scoring

This response earns no credit (0 points) because the student did not determine the correct proportional relationship. The student may have subtracted 8 from 12 to get 4 , not realizing that this item is asking for the proportional relationship between quantities.

## Sample Response: 0 points

A dance studio offers ballet and hip-hop classes. The studio has 8 ballet classes for every 12 hip-hop classes. How many hip-hop classes are there for each ballet class?
0.6


## Notes on Scoring

This response earns no credit (0 points) because the student did not determine the correct proportional relationship. The student may have calculated the proportional relationship between the number of hip-hop classes to the total number of classes, calculating $12 / 20$ to get 0.6 .

# Grade 7 Math <br> Spring 2016 Item Release 

Question 13

## Question and Scoring Guidelines

## Question 13

One apple costs $\$ 0.55$ at the grocery store. Customers receive one free apple for every 8 apples that they buy. Anna paid a total of $\$ 8.80$ for her apples.

How many free apples did Anna receive?


## Points Possible: 1

Content Cluster: Solve real-life and mathematical problems using numerical and algebraic expressions and equations.

Content Standard: Use variables to represent quantities in a realworld or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities.
a. Solve word problems leading to equations of the form $p x+q=r$ and $p(x+q)=r$, where $p, q$, and $r$ are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm . Its length is 6 cm . What is its width? (7.EE.4a)

Calculator Designation: Calculator

## Scoring Guidelines

Exemplar Response

- 2


## Other Correct Responses

- N/A

For this item, a full-credit response includes:

- The correct value (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 13

Sample Responses

## Sample Response: 1 point

```
One apple costs $0.55 at the grocery store. Customers receive one free apple for every 8 apples that they buy. Anna paid a total of $8.80 for her
apples.
How many free apples did Anna receive?
2
\leftarrow}->
|1
```


## Notes on Scoring

This response earns full credit (1 point) because the student determined the correct value. The student may have divided the total cost of $\$ 8.80$ by the cost per apple, $\$ 0.55$, to find that Anna buys 16 apples. The student may have then realized that there are 2 groups of 8 apples and that Anna gets 1 apple per 8 apples, which gives her 2 free apples.

## Sample Response: 0 points

```
One apple costs $0.55 at the grocery store. Customers receive one free apple for every 8 apples that they buy. Anna paid a total of $8.80 for her
apples.
How many free apples did Anna receive?
```

    16
    \(\oplus \oplus \rightarrow(\)
    \begin{tabular}{|l|l|l|}
    \hline 1 \& 2 \& 3 <br>
\hline
\end{tabular}

| 4 | 5 | 6 |
| :--- | :--- | :--- |


| 7 | 8 | 9 |
| :--- | :--- | :--- |


| 0 | . | - |
| :--- | :--- | :--- |

## Notes on Scoring

This response earns no credit (0 points) because the student did not determine the correct value. The student may have correctly calculated how many apples Anna bought and then answered with 16, not remembering that the question was about how many free apples she received.

## Sample Response: 0 points

One apple costs $\$ 0.55$ at the grocery store. Customers receive one free apple for every 8 apples that they buy. Anna paid a total of $\$ 8.80$ for her
apples.
How many free apples did Anna receive?

| 3.85 |  |  |
| :--- | :--- | :--- |
|  |  |  |
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

## Notes on Scoring

This response earns no credit (0 points) because the student did not determine the correct value. The student may have thought that for every 8 apples, 1 is free, which means that you only pay for 7 apples. Then, the student may have calculated the cost of 7 apples: $0.55 * 7=3.85$.

# Grade 7 Math <br> Spring 2016 Item Release 

Question 14

Question and Scoring Guidelines

## Question 14

The circumference of a circle is 18.84 inches.
What is the diameter of the circle, to the nearest inch?


## Points Possible: 1

Content Cluster: Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.

Content Standard: Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle. (7.G.4)

Calculator Designation: Calculator

## Scoring Guidelines

Exemplar Response

- 6


## Other Correct Responses

- Any value between 5.99 and 6

For this item, a full-credit response includes:

- A correct diameter (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 14

Sample Responses

## Sample Response: 1 point

The circumference of a circle is 18.84 inches.
What is the diameter of the circle, to the nearest inch?

## 6



## Notes on Scoring

This response earns full credit (1 point) because the student determined the correct diameter of the circle. The student may have applied the formula for the circumference of a circle $(2 * \pi * r=C)$ to find the diameter of the circle, understanding that $2 * r$ is equal to the diameter. Then, the student would have only needed to divide 18.84 by $\pi$, using $3.14,22 / 7$ or the $\pi$-button on a calculator for the value of Pi. Finally, the student correctly rounded the answer to the nearest inch.

## Sample Response: 0 points

The circumference of a circle is 18.84 inches.
What is the diameter of the circle, to the nearest inch?

## 9



## Notes on Scoring

This response earns no credit ( 0 points) because the student did not determine the correct diameter of the circle. The student may have misunderstood the formula for the circumference of a circle $(2 * \pi * r=C)$ by thinking that $\pi * r$ is the diameter, and therefore divided 18.84 by 2 to get 9.42 . The student may have then rounded to the nearest inch to get 9 .

## Sample Response: 0 points

The circumference of a circle is 18.84 inches.
What is the diameter of the circle, to the nearest inch?

### 4.89



5


8 9

0 $\square$


## Notes on Scoring

This response earns no credit (0 points) because the student did not determine the correct diameter of the circle. The student may have used the formula for the area of the circle, $\pi r^{2}=A$, instead of the formula for the circumference of the circle, $2 \pi r=C$, to calculate the length of the radius, and then multiplied by 2 to get the diameter.

# Grade 7 Math <br> Spring 2016 Item Release 

Question 15
Question and Scoring Guidelines

## Question 15

A bread company makes wheat dough and rye dough each day. The company makes 15.2 pounds of wheat dough for every 9.5 pounds of rye dough

How many pounds of wheat dough does the company make for each pound of rye dough?


## Points Possible: 1

Content Cluster: Analyze proportional relationships and use them to solve real-world and mathematical problems.

Content Standard: Recognize and represent proportional relationships between quantities.
b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. (7.RP.2b)

Calculator Designation: Calculator

## Scoring Guidelines

## Exemplar Response

- 1.6


## Other Correct Responses

- N/A

For this item, a full-credit response includes:

- The correct value (1 point).


# Grade 7 Math <br> Spring 2016 Item Release 

Question 15

Sample Responses

## Sample Response: 1 point



## Notes on Scoring

This response earns full credit (1 point) because the student determined the correct value. The student may have recognized the proportional relationship and divided 15.2 by 9.5 to get 1.6 pounds of wheat dough per 1 pound of rye dough.

## Sample Response: 0 points



## Notes on Scoring

This response earns no credit (0 points) because the student did not determine the correct value. The student may not have recognized the proportional relationship and instead subtracted 9.5 from 15.2 to get 5.7.

## Sample Response: 0 points



## Notes on Scoring

This response earns no credit (0 points) because the student did not determine the correct value. The student may have reversed the proportional relationship and instead answered how many pounds of rye dough the company makes per 1 pound of wheat dough.

# Grade 7 Math <br> Spring 2016 Item Release 

Question 16

Question and Scoring Guidelines

## Question 16

The tables show the cost for different numbers of song downloads.
Which table shows a proportional relationship?

(A) \begin{tabular}{|c|c|}

\hline | Number of |
| :---: |
| Songs | \& Cost <br>

\hline 2 \& $\$ 3.50$ <br>
\hline 4 \& $\$ 7.00$ <br>
\hline 5 \& $\$ 8.75$ <br>
\hline 7 \& $\$ 13.25$ <br>
\hline
\end{tabular}

(c)

| Number of <br> Songs | Cost |
| :---: | :---: |
| 2 | $\$ 3.50$ |
| 4 | $\$ 8.00$ |
| 5 | $\$ 8.75$ |
| 7 | $\$ 13.25$ |

B

| Number of <br> Songs | Cost |
| :---: | :---: |
| 2 | $\$ 3.50$ |
| 4 | $\$ 8.00$ |
| 5 | $\$ 8.75$ |
| 7 | $\$ 12.25$ |

(D)

| Number of <br> Songs | Cost |
| :---: | :---: |
| 2 | $\$ 3.50$ |
| 4 | $\$ 7.00$ |
| 5 | $\$ 8.75$ |
| 7 | $\$ 12.25$ |

## Points Possible: 1

Content Cluster: Analyze proportional relationships and use them to solve real-world and mathematical problems.

Content Standard: Recognize and represent proportional relationships between quantities.
a. Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.
(7.RP.2a)

Calculator Designation: Calculator

## Scoring Guidelines

Rationale for Option A: This is incorrect. The student may have thought that since $3.5 / 2=7 / 4=8.75 / 5$, then there is a proportional relationship for the table, but the student did not include 13.25/7, which is not the same ratio as the others.

Rationale for Option B: This is incorrect. The student may have found that some values in the table have the same ratio of cost per number of songs, but the student did not check all of the values in the table.

Rationale for Option C: This is incorrect. The student may have found that some values in the table have the same ratio of cost per number of songs, but the student did not check all of the values in the table.

Rationale for Option D: Key - The student correctly identified the table with numbers showing a proportional relationship (12.25/7 $=1.75$ ), $(8.75 / 5=1.75)$, $(7 / 4=1.75)$ and $(3.5 / 2=1.75)$.

## Sample Response: 1 point

The tables show the cost for different numbers of song downloads.
Which table shows a proportional relationship?
(A)

| Number of <br> Songs | Cost |
| :---: | :---: |
| 2 | $\$ 3.50$ |
| 4 | $\$ 7.00$ |
| 5 | $\$ 8.75$ |
| 7 | $\$ 13.25$ |

(c)

| Number of <br> Songs | Cost |
| :---: | :---: |
| 2 | $\$ 3.50$ |
| 4 | $\$ 8.00$ |
| 5 | $\$ 8.75$ |
| 7 | $\$ 13.25$ |

(B) \begin{tabular}{|c|c|}

\hline | Number of |
| :---: |
| Songs | \& Cost <br>

\hline 2 \& $\$ 3.50$ <br>
\hline 4 \& $\$ 8.00$ <br>
\hline 5 \& $\$ 8.75$ <br>
\hline 7 \& $\$ 12.25$ <br>
\hline
\end{tabular}

| Number of <br> Songs | Cost |
| :---: | :---: |
| 2 | $\$ 3.50$ |
| 4 | $\$ 7.00$ |
| 5 | $\$ 8.75$ |
| 7 | $\$ 12.25$ |

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