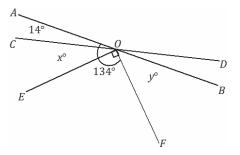
Lesson 3: Solving for Unknown Angles Using Equations

Classwork

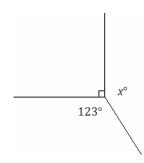
Opening Exercise

Two lines meet at a point that is also the vertex of an angle; the measurement of $\angle AOF$ is 134°. Set up and solve an equation to find the values of x and y. Are your answers reasonable? How do you know?



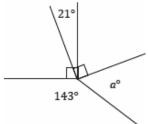
Example 1

Set up and solve an equation to find the value of *x*.



Exercise 1

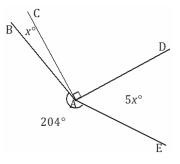
Five rays meet at a common endpoint. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of a.





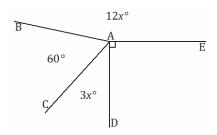
Example 2

Four rays meet at a common endpoint. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of x. Find the measurements of $\angle BAC$ and $\angle DAE$.



Exercise 2

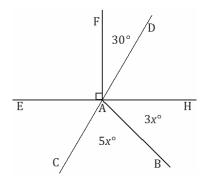
Four rays meet at a common endpoint. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of x. Find the measurement of $\angle CAD$.





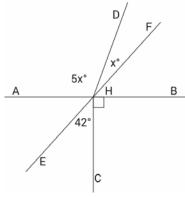
Example 3

Two lines meet at a point that is also the endpoint of two rays. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of x. Find the measurements of $\angle BAC$ and $\angle BAH$.



Exercise 3

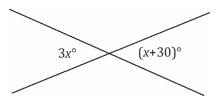
Lines *AB* and *EF* meet at a point which is also the endpoint of two rays. In a complete sentence, describe the relevant angle relationships in the diagram. Set up and solve an equation to find the value of x. Find the measurements of $\angle DHF$ and $\angle AHD$.





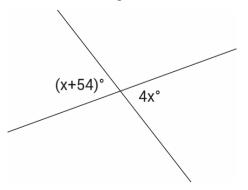
Example 4

Two lines meet at a point. Set up and solve an equation to find the value of x. Find the measurement of one of the vertical angles.



Exercise 4

Set up and solve an equation to find the value of x. Find the measurement of one of the vertical angles.





Lesson Summary

Steps to Solving for Unknown Angles

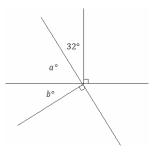
- Identify the angle relationship(s).
- Set up an equation that will yield the unknown value.
- Solve the equation for the unknown value.
- Substitute the answer to determine the angle(s).
- Check and verify your answer by measuring the angle with a protractor.

Problem Set

1. Two lines meet at a point. Set up and solve an equation to find the value of *x*.

2. Three lines meet at a point. Set up and solve an equation to find the value of *a*. Is your answer reasonable? Explain how you know.

3. Two lines meet at a point that is also the endpoint of two rays. Set up and solve an equation to find the values of aand b.



78°

a

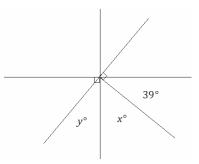
52°

72°

(x+15)°



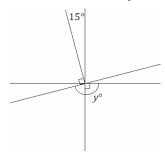
4. Three lines meet at a point that is also the endpoint of a ray. Set up and solve an equation to find the values of *x* and *y*.



3*x*°

Lesson 3

- Two lines meet at a point. Find the measurement of one of the vertical angles. Is your answer reasonable? Explain how you know.
- 6. Three lines meet at a point that is also the endpoint of a ray. Set up and solve an equation to find the value of *y*.



- 7. Three adjacent angles are at a point. The second angle is 20° more than the first, and the third angle is 20° more than the second angle.
 - a. Find the measurements of all three angles.
 - b. Compare the expressions you used for the three angles and their combined expression. Explain how they are equal and how they reveal different information about this situation.
- 8. Four adjacent angles are on a line. The measurements of the four angles are four consecutive even numbers. Determine the measurements of all four angles.
- 9. Three adjacent angles are at a point. The ratio of the measurement of the second angle to the measurement of the first angle is 4:3. The ratio of the measurement of the third angle to the measurement of the second angle is 5:4. Determine the measurements of all three angles.





10. Four lines meet at a point. Solve for *x* and *y* in the following diagram.

